

**Computing and Software 734**  
**Formalized Mathematics**  
**Winter 2008**

**Exercise 10**

**20 pts.**

**Due 16 April 2008**

Assigned: 7 March 2008

Revised: 7 March 2008

This exercise is not required; it is for extra credit.

**Part 1**

Starting from scratch, create an IMPS theory of Peano arithmetic called `peano2` with the constants `0` and `S` and the following axioms:

1. `0` is not a successor.
2. `S` is injective.
3. Induction.

**Part 2**

Define `+` and `*` recursively in `peano2` using `def-recursive-constant`.

**Part 3**

Do parts 2–4 of Exercise 8 using `peano2` in place of `peano1`.